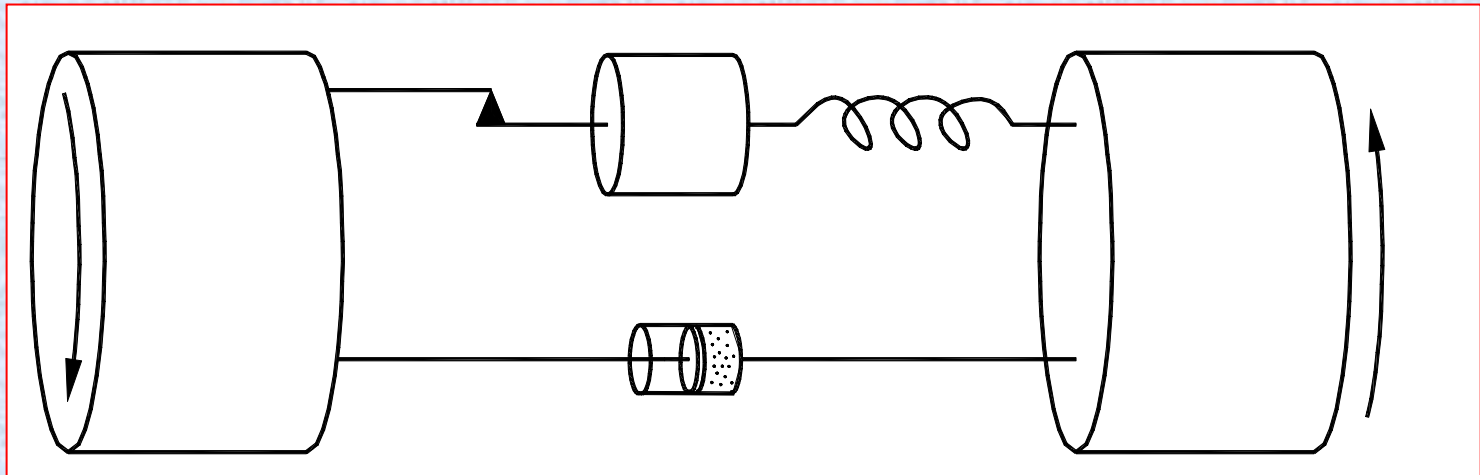
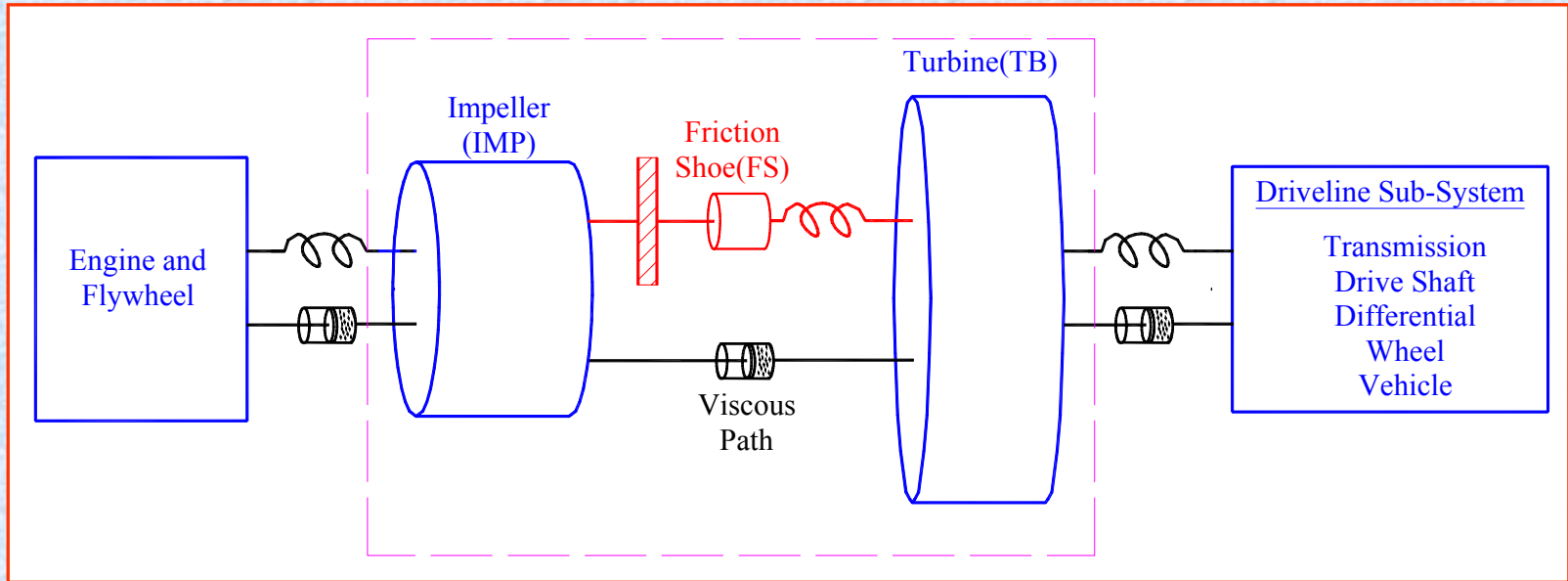


# Dynamic Analysis of Dry Friction Paths in Torsional Systems *With Focus on Automotive Torque Converter Clutch*

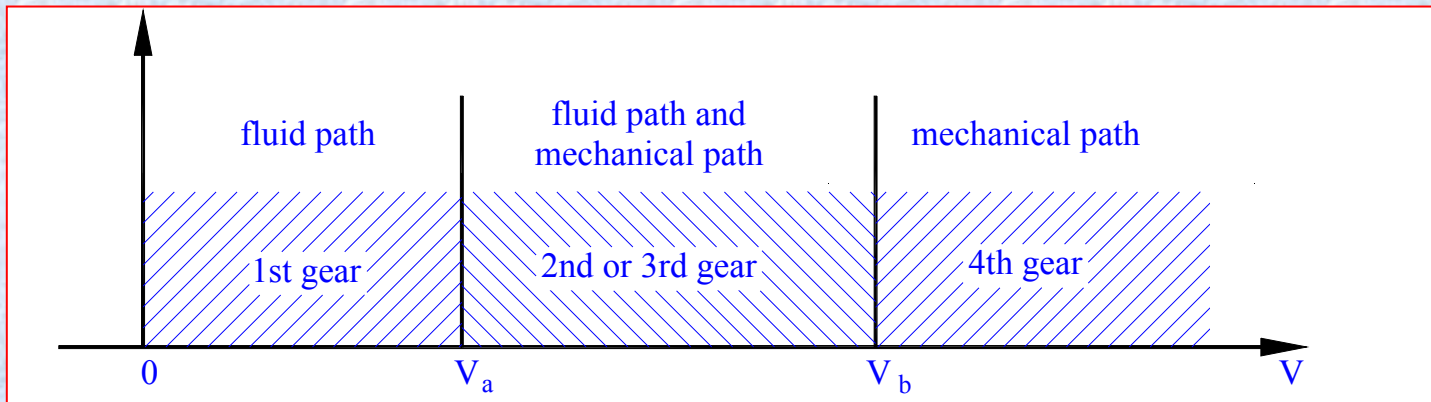
**C. Duan and R. Singh**



# Automotive Drive Train: System and Operating Conditions

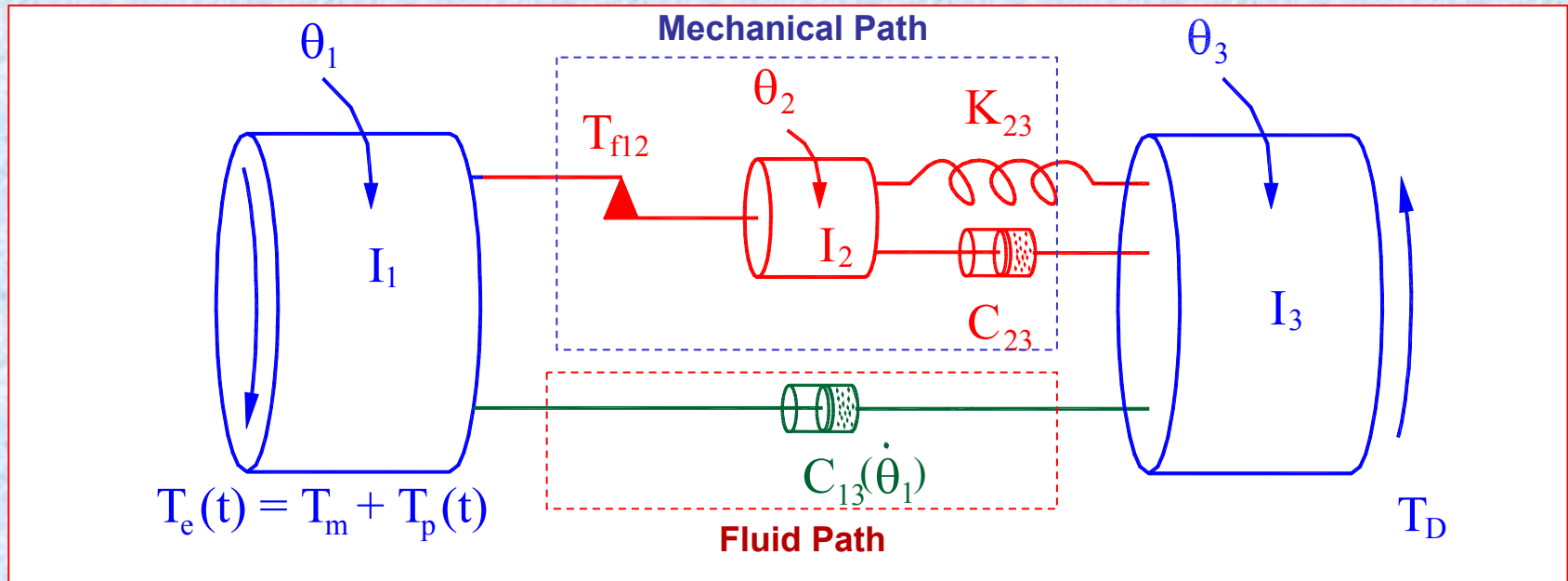


**Schematic Model**



**TCC Operating Conditions**

# Reduced Order System



$I_1$ : Flywheel and Impeller

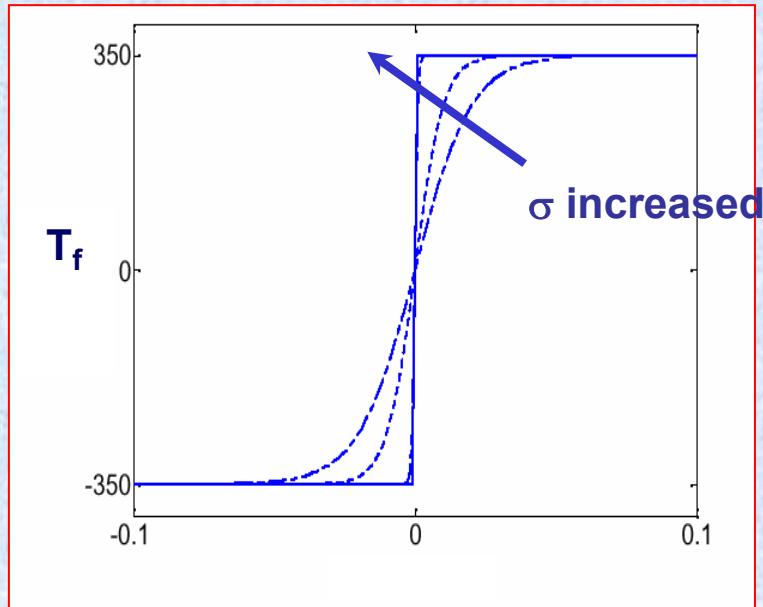
$I_2$ : Friction Shoe Assembly

$I_3$ : Downstream Driveline

- Engine torque: combination of mean and pulsating terms
- Dry friction clutch: non-linear torque w.r.t interfacial relative velocity
- Fluid (viscous) path: torque transmitted w.r.t. engine speed

# Smoothened vs. Discontinuous Coulomb Friction Formulation

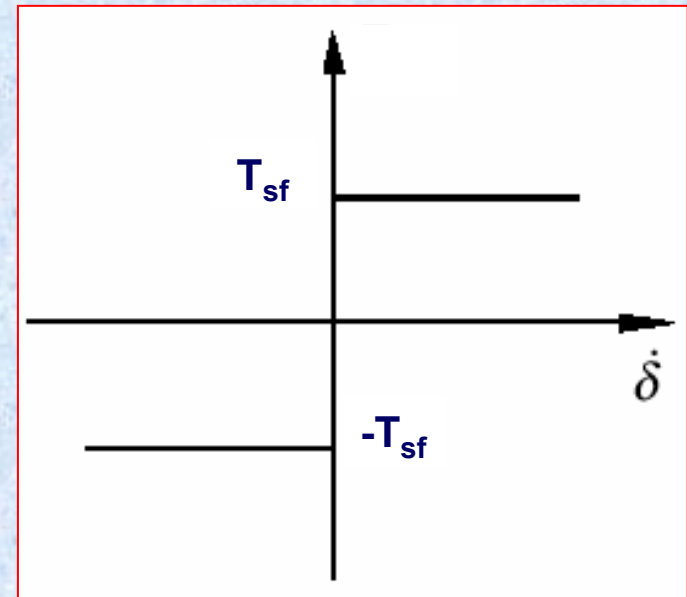
## Continuous and Non-linear:



$\sigma$  = conditioning factor

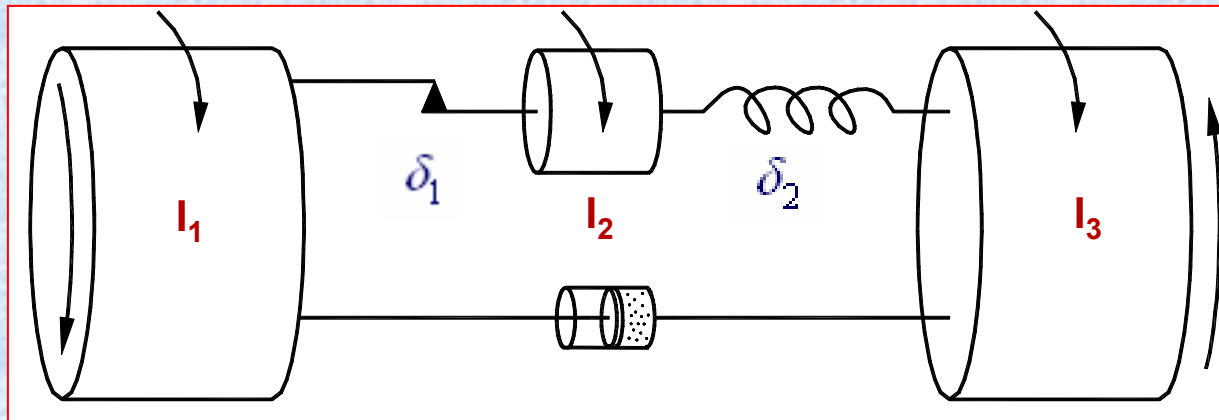
- Active friction torque w.r.t. relative velocity

## Discontinuous and Piecewise Linear:

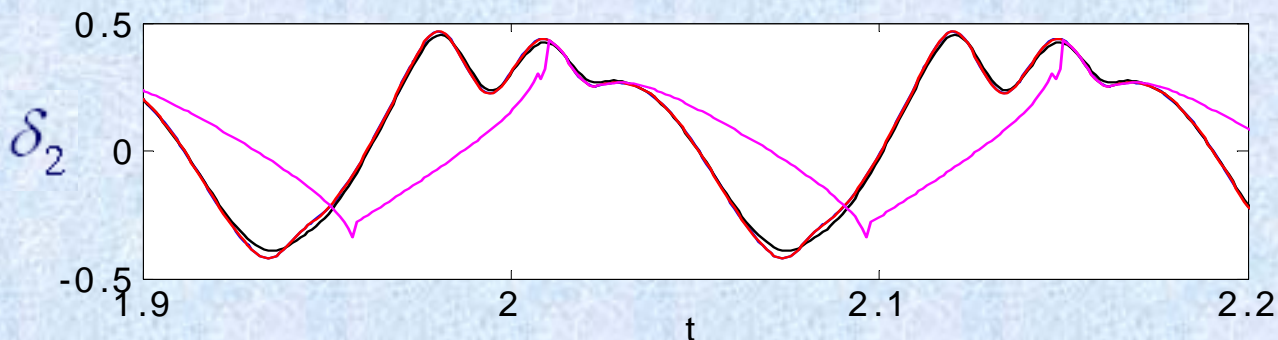
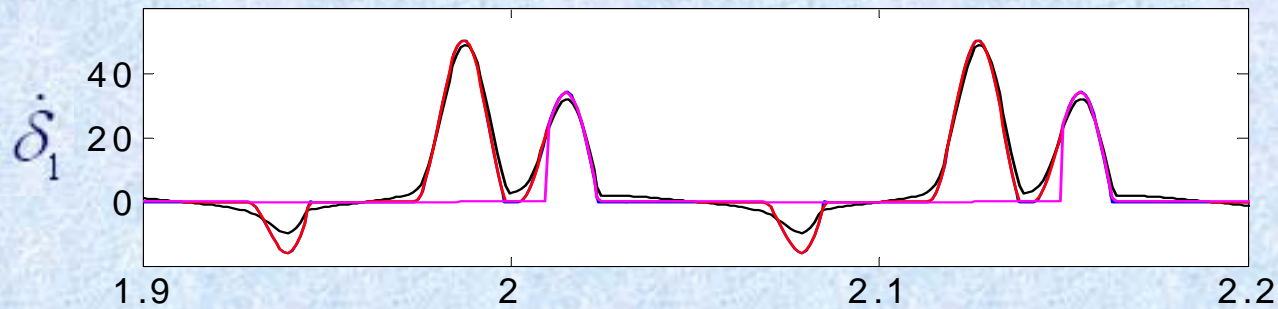


- Passive friction torque w.r.t. relative velocity

## Smoothened vs. Discontinuous Friction Formulations



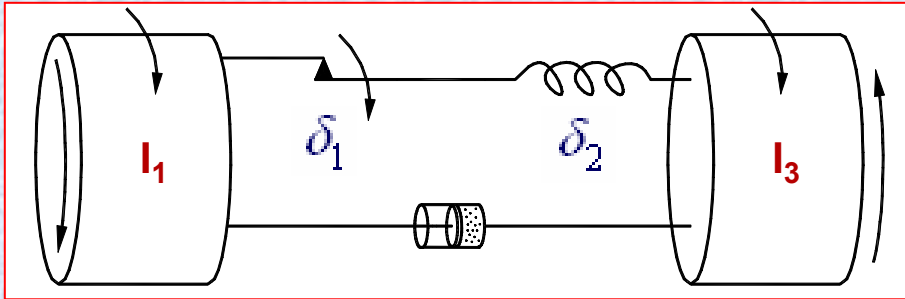
### • Time Domain Responses:



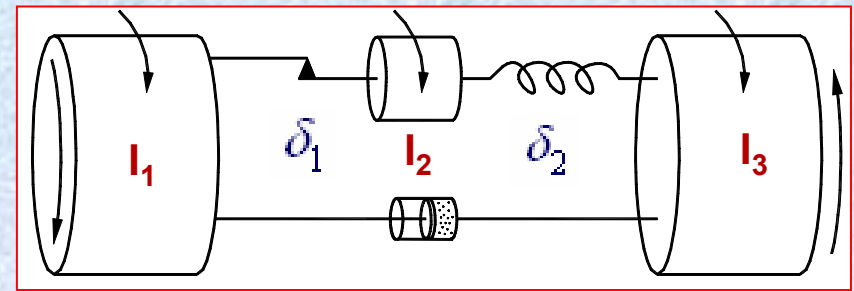
— discontinuous friction; 
 — smoothed  $\sigma = 0.5$ ; 
 — smoothed  $\sigma = 10^2$ ; 
 — smoothed  $\sigma = 10^3$

# Effect of Secondary Mass: 2DOF vs. 3DOF Systems

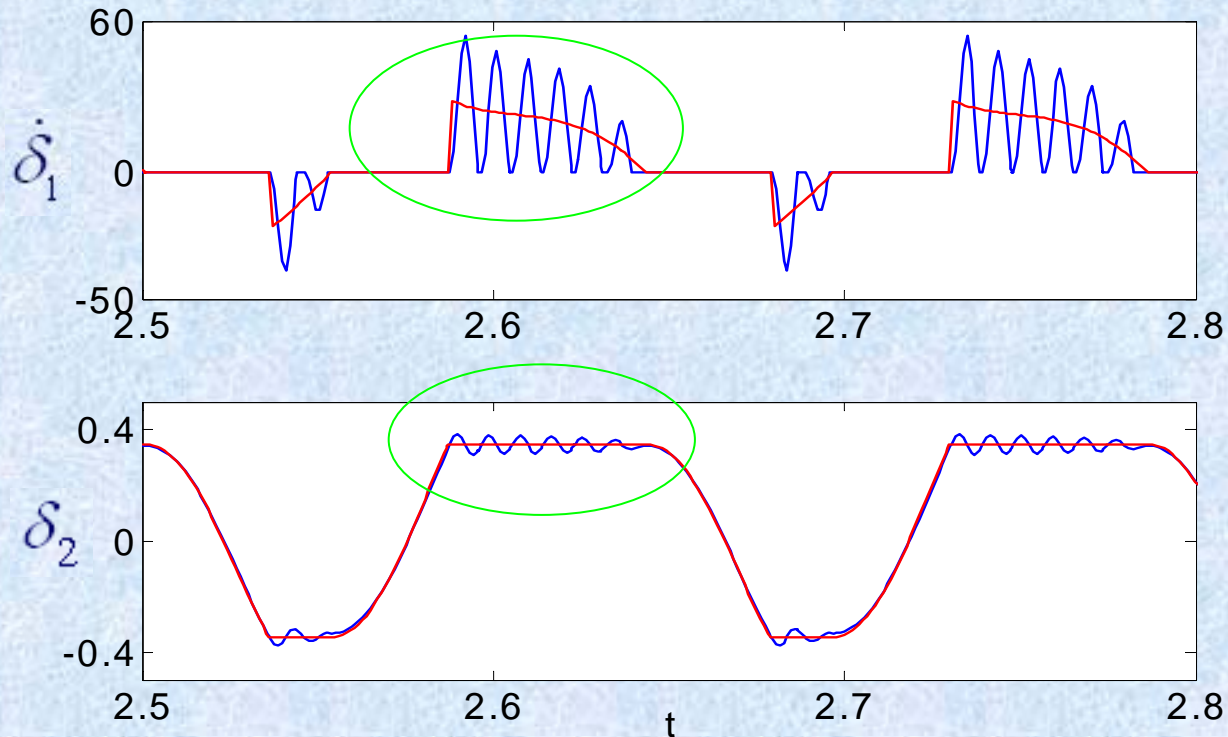
**2DOF ( $I_2 = 0$ )**



**3DOF ( $I_2 \neq 0$ )**

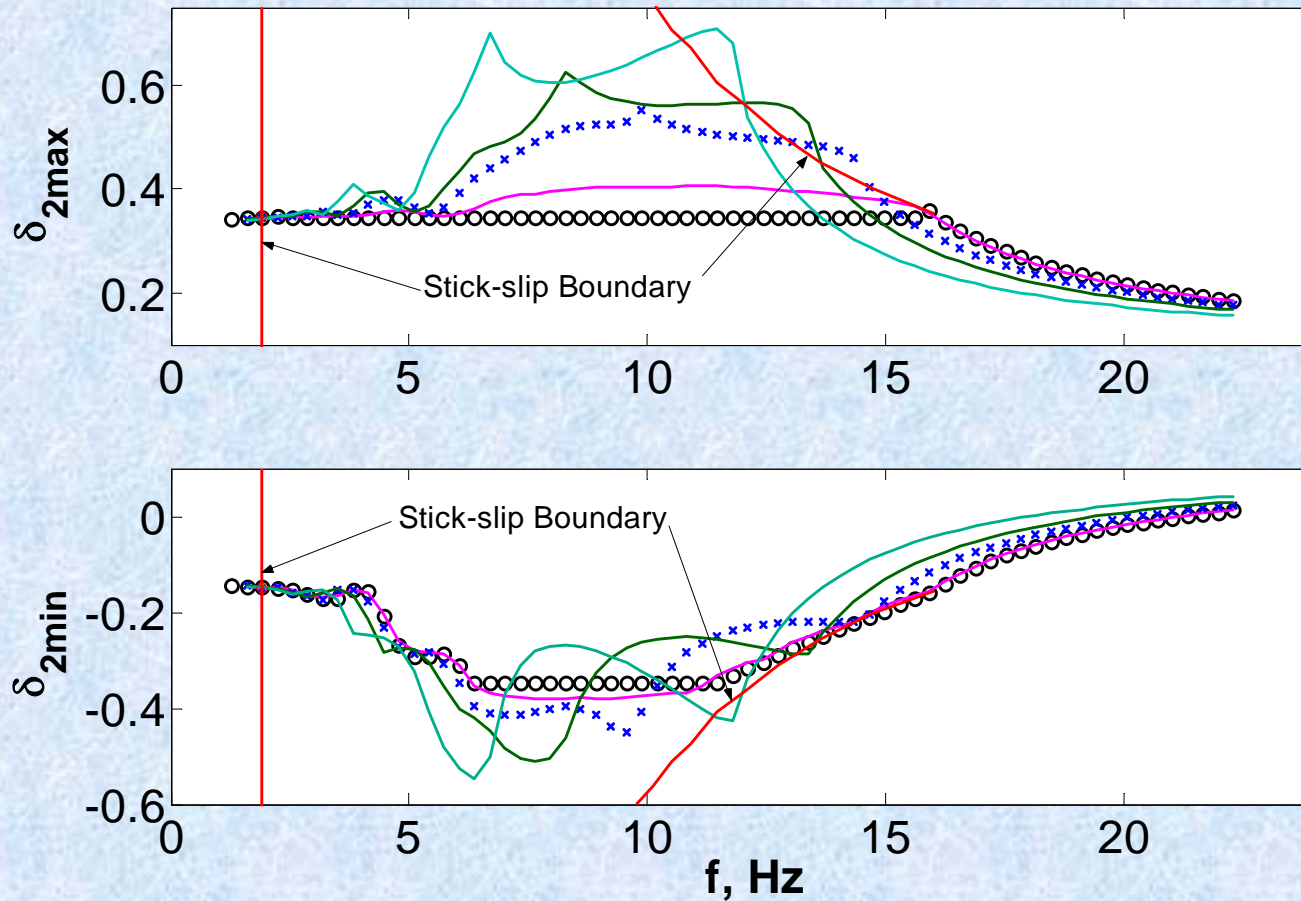


• **Comparison of Time Histories**



**Key:** —  $I_2/I_1 = 0$ ; —  $I_2/I_1 = 0.01$

# Frequency Response Characteristics: 2DOF vs. 3DOF System

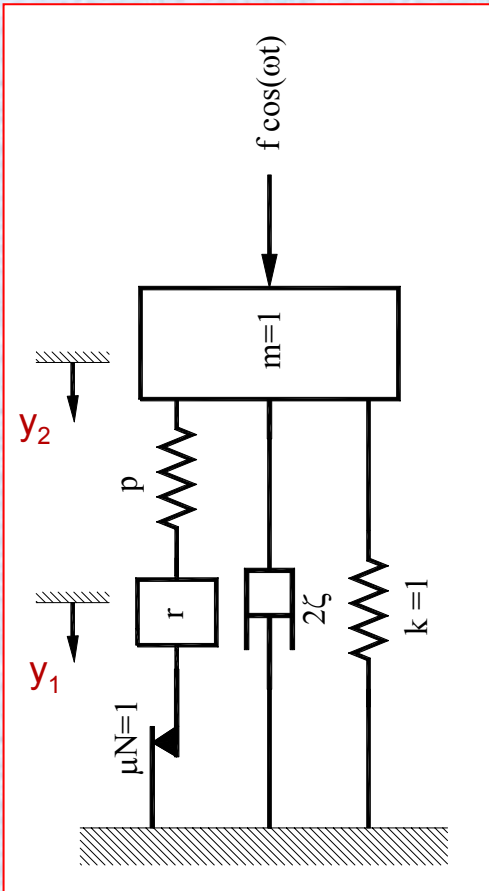


**Key:**

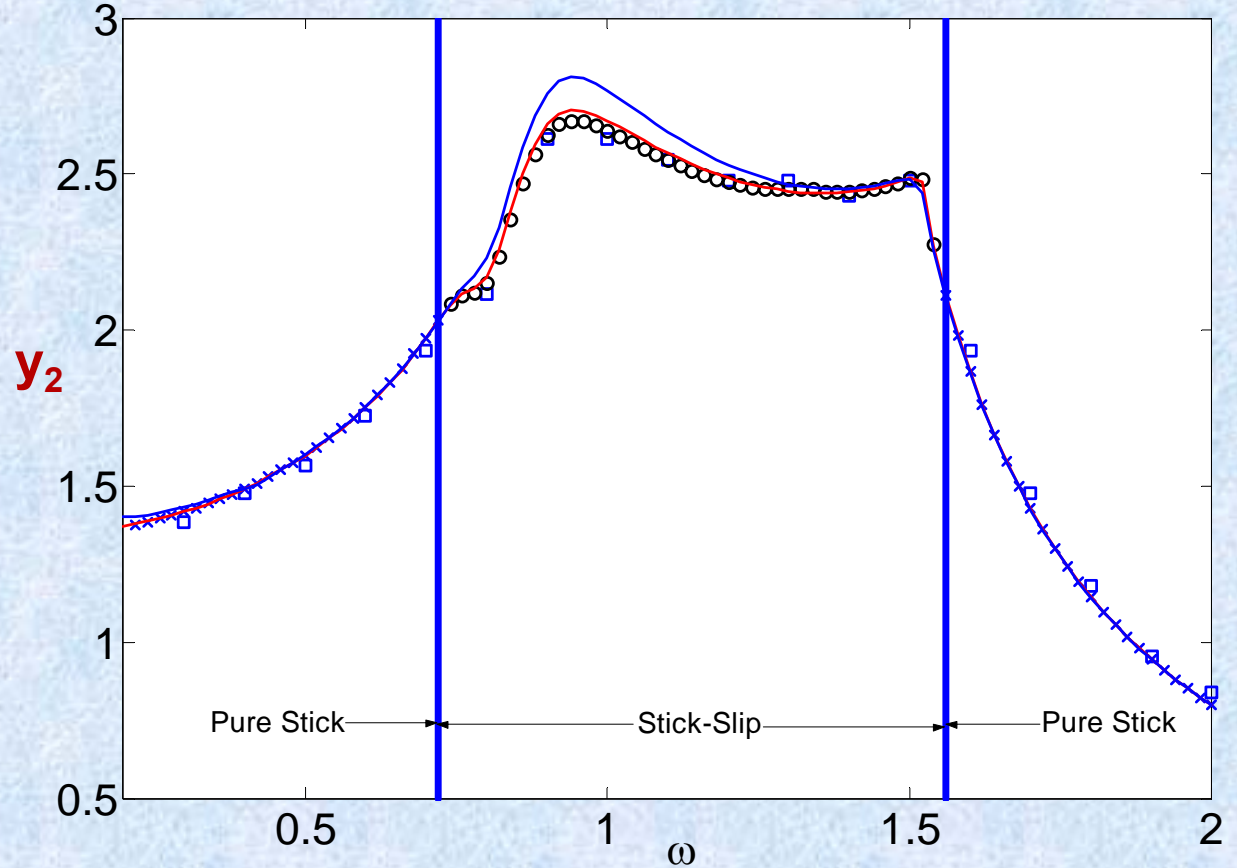
- o o o  $I_2/I_1 = 0$  (2DOF)
- x x x  $I_2/I_1 = 0.1$
- $I_2/I_1 = 0.4$
- $I_2/I_1 = 0.01$
- $I_2/I_1 = 0.2$
- Boundaries based on the linear theory



## Validation: Ferri and Heck's Analysis (1995)



**Turbine Blade  
Friction Damper**



**Key:**

**x x x** pure stick solution

**o o o** discontinuous model

**—** smoothed friction  $\sigma = 50$

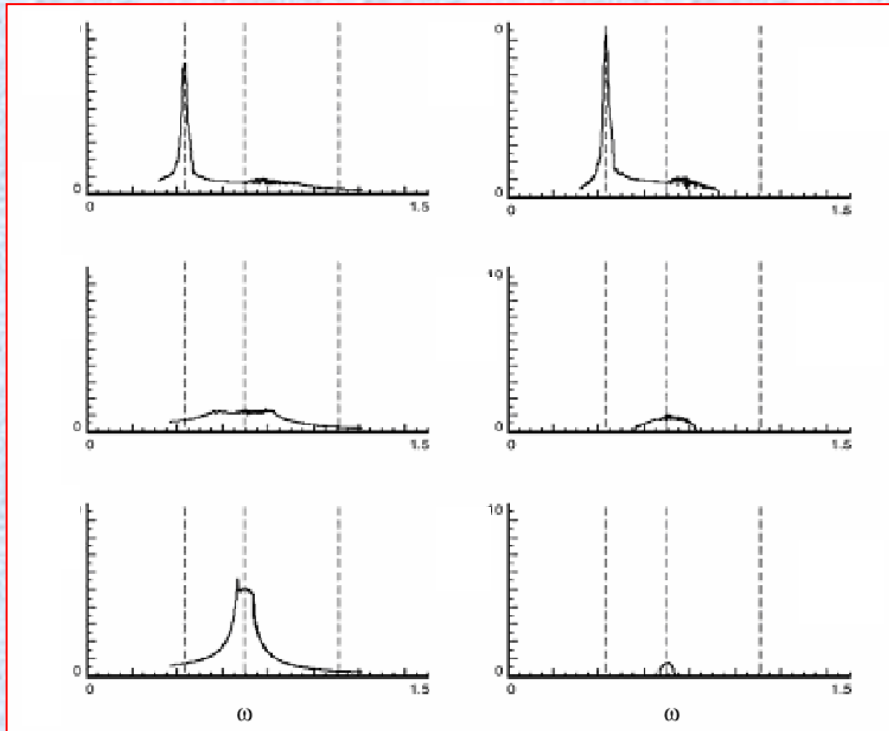
**—** smoothed friction  $\sigma = 10$

**□ □ □** Ferri and Heck's

# Validation: Hartung et. al. Experiment (2001)

$\xi_1$

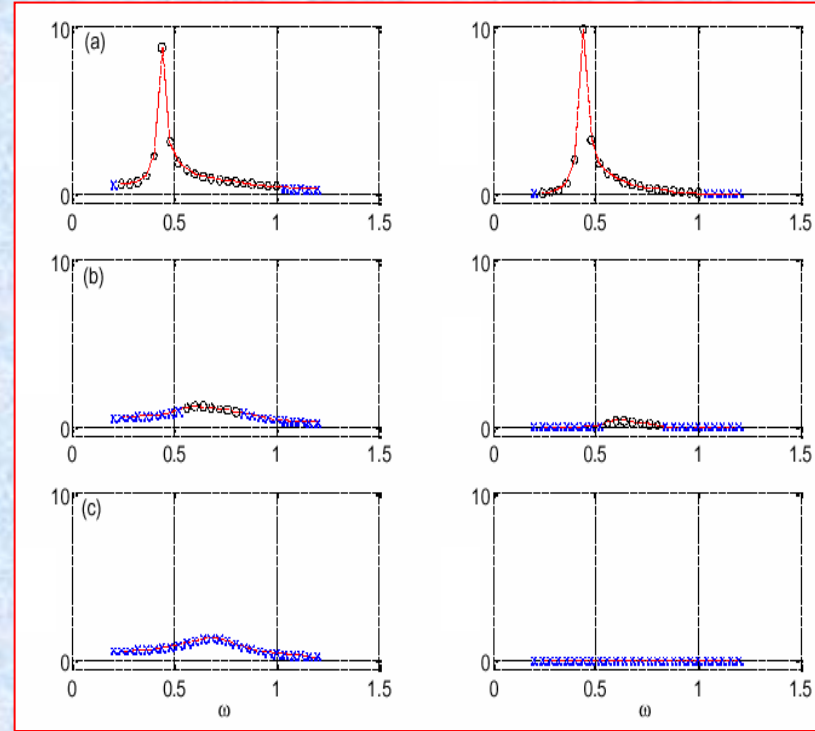
$\xi_2$



Hartung et. al. Experiment (2001)

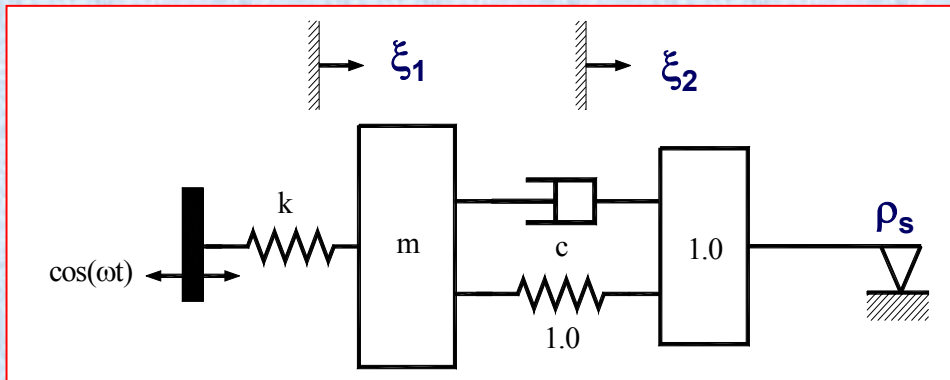
$\xi_1$

$\xi_2$



Our Predictions

$\rho_s \uparrow$



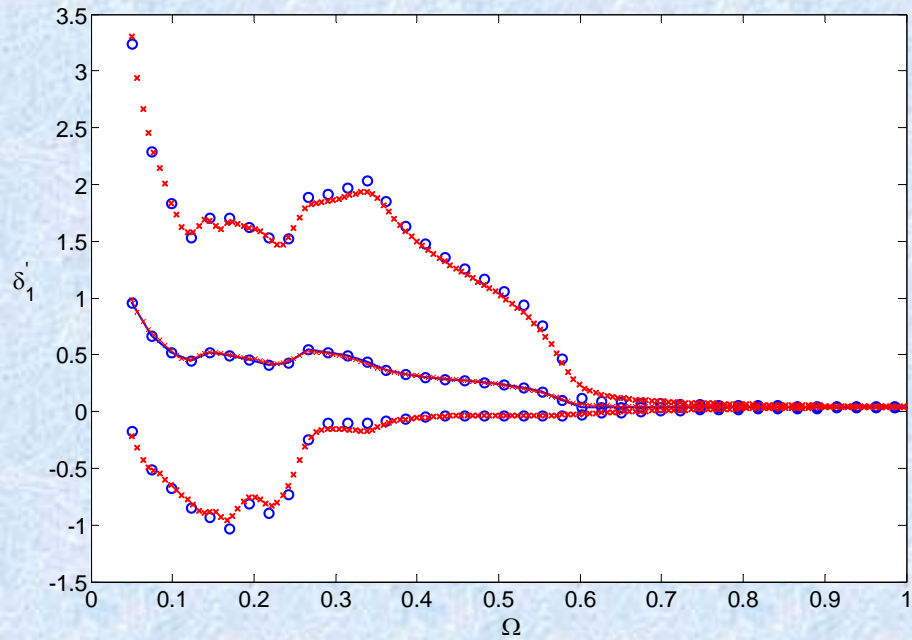
**Key:**

**x x x** pure stick solution

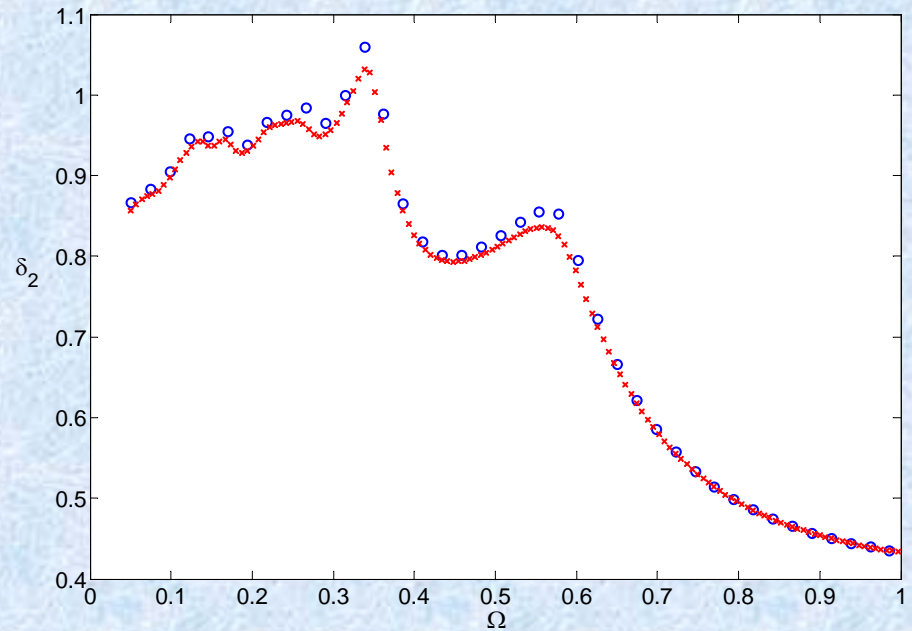
**o o o** discontinuous solution

**—** smoothed friction  $\sigma = 50$

# Non-Linear Frequency Response Characteristics Appearance of Super-Harmonics



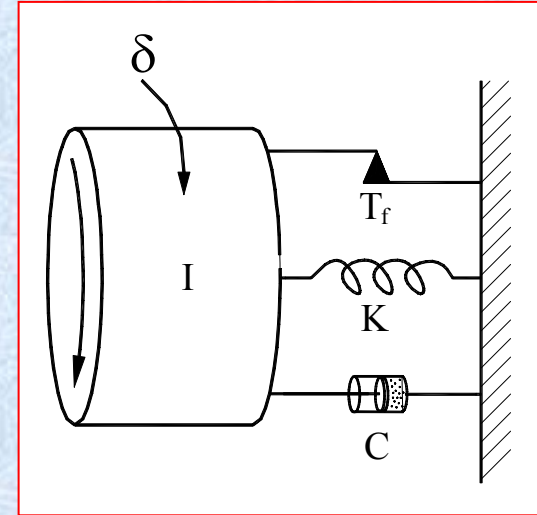
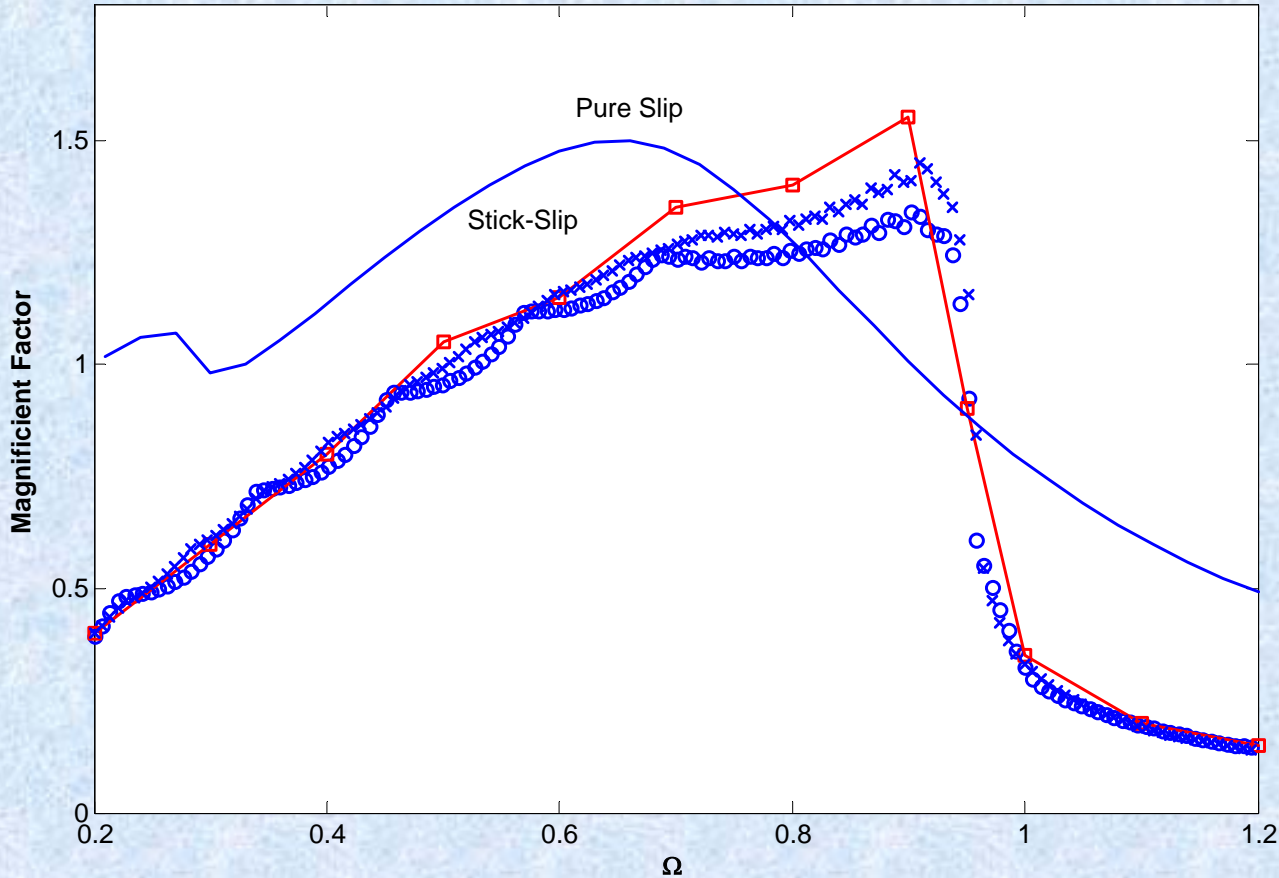
Velocity ( $\theta_1 - \theta_2$ ): max-mean-min



Displacement ( $\theta_2$ ): rms

Key:  $\circ \circ \circ$  Broyden;  $\times \times \times$  Newton Raphson

# Comparison with Den Hartog's Model



- □ -: Den Hartog's model
- ooo: MHMB(12 Harmonics)
- xxx: MHBM(24 Harmonics)
- : slip motion boundary



**MHBM = Multi-term Harmonic Balance Method**



## Publications

1. C. Duan and R. Singh, *Dynamics of a 3DOF Torsional System with a Dry Friction Controlled Path*, submitted to the Journal of Sound and Vibration, 2003.
2. C. Duan and R. Singh, *Super-Harmonics in a Torsional System with Dry Friction Path Subject to Harmonic Excitation under a Mean Torque*, submitted to the Journal of Sound and Vibration, 2004.
3. C. Duan and R. Singh, *Effect of Time-Varying Dry Friction on Transient and Steady-State Responses of a Torsional System*, in preparation for the Journal of Sound and Vibration, 2004.